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National

## Applications of Mathematics

Paper 2

THURSDAY, 2 MAY
10:35 AM - 12:35 PM

Fill in these boxes and read what is printed below.

Full name of centre
$\square$


Forename(s)
Surname
Number of seat


Date of birth
Day

|  | Month | Year | Scottish candidate number |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Total marks - 65
Attempt ALL questions.

## You may use a calculator.

To earn full marks you must show your working in your answers.
State the units for your answer where appropriate.
Write your answers clearly in the spaces provided in this booklet. Additional space for answers is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting.
Use blue or black ink.
Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.

## FORMULAE LIST

| Circumference of a circle | $C=\pi d$ |
| :--- | :--- |
| Area of a circle | $A=\pi r^{2}$ |

Theorem of Pythagoras


$$
a^{2}+b^{2}=c^{2}
$$

Volume of a cylinder

$$
V=\pi r^{2} h
$$

Volume of a prism

$$
V=A h
$$

Volume of a cone

$$
V=\frac{1}{3} \pi r^{2} h
$$

Volume of a sphere

$$
V=\frac{4}{3} \pi r^{3}
$$

Standard deviation $\quad s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}$
or $s=\sqrt{\frac{\Sigma x^{2}-\frac{(\Sigma x)^{2}}{n}}{n-1}}$, where $n$ is the sample size.

Gradient


$$
\text { gradient }=\frac{\text { vertical height }}{\text { horizontal distance }}
$$

## Total marks - 65

Attempt ALL questions

1. Sam buys a rare stamp for his stamp collection at an auction. He buys the stamp for $£ 920$.

The stamp

- increased in value by $7 \%$ in each of the first 2 years
- decreased in value by $4 \%$ in the third year.

Calculate the value of the stamp after these 3 years.
Give your answer to 3 significant figures.
2. A bottle consists of a cuboid and a cylinder.

The dimensions are shown in the diagram.


Calculate the volume of the bottle.
3. The graph shows how many pounds sterling could be bought for 1 euro during December 2017.

Exchange rate
pounds
sterling
per euro


Daniel changed 250 euros to pounds sterling at 09:00 on 7 December.
(a) Calculate how many pounds he received.

Daniel was working in France.
He bought a laptop costing 400 euros.
He calculated this was equivalent to $£ 334 \cdot 80$.
(b) Use the graph to find the date that Daniel bought the laptop.

Use your working to justify your answer.
4. Karen buys and sells silver, gold and platinum.

The table shows the price per ounce of each of these metals, on the first trading day of each month, over the last year.

| Month | Price of silver | Price of gold | Price of platinum |
| :--- | :---: | :---: | :---: |
| Jan | $15 \cdot 60$ | 1170 | 1275 |
| Feb | $17 \cdot 40$ | 1140 | 1050 |
| Mar | $16 \cdot 50$ | 1210 | 1100 |
| Apr | $17 \cdot 00$ | 1200 | 1150 |
| May | $16 \cdot 70$ | 1190 | 1100 |
| Jun | $16 \cdot 70$ | 1275 | 1075 |
| Jul | 14.50 | 1175 | 1100 |
| Aug | 14.50 | 1140 | 1125 |
| Sep | $15 \cdot 60$ | 1195 | 1000 |
| Oct | 16.50 | 1200 | 1125 |
| Nov | All prices in US dollars | 1200 |  |
| Dec |  |  |  |
|  |  |  |  |

Karen bought 1 ounce of gold on the first trading day in March and sold it on the first trading day in September.
Calculate the percentage loss she made.
Give your answer to 2 decimal places.
5. A hotel is having a swimming pool built.

It is in the shape of a rectangle and two quarter circles as shown below.


The swimming pool will have a safety rail fitted around its edge.

- There will be two 125 cm wide gaps to allow access to the pool
- Safety rail is sold in 3 metre lengths
- Each 3 metre length costs $£ 11.49$

Calculate the minimum cost of the safety rail for the pool.
6. Denisa bought 375 shares for $£ 4 \cdot 50$ per share.

She later sold them all for $£ 5 \cdot 20$ per share.
She had to pay commission of $2 \cdot 7 \%$ of the total selling price.
Calculate her total profit.
7. The birth weight of babies in a hospital in 2017 was recorded.

A sample of the weights, in kilograms, is shown.

$$
\begin{array}{llllll}
2.5 & 4.5 & 3.7 & 3.1 & 3.8 & 3.4
\end{array}
$$

(a) For these weights, calculate
(i) the mean
(ii) the standard deviation.

The birth weight of babies born in hospital in 1987 was also recorded. The mean weight in 1987 was 3.4 kg and the standard deviation was 0.95 kg .
(b) Make two valid comparisons about the weight of babies in 1987 and 2017.

## 7. (continued)

The lengths and weights of 8 new-born babies are recorded in the table as shown.

| Length (cm) | 46 | 47 | 49 | 51 | 52 | 52 | 54 | 55 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight (kg) | $2 \cdot 7$ | $2 \cdot 8$ | $3 \cdot 5$ | $3 \cdot 7$ | $3 \cdot 4$ | $3 \cdot 7$ | $4 \cdot 0$ | 4.4 |

(c) (i) On the grid draw a scatter graph to show this data.
(An additional grid, if required, can be found on page 20.)

(ii) Draw a line of best fit on your scatter graph.
(iii) Use your line of best fit to estimate the weight of a baby who was 50 cm when born.

## 7. (continued)

Baby milk powder is sold in 900 g packs.
The feeding guide from one of these packs is shown.

| Approximate <br> baby weight <br> (kg) | Number of <br> feeds per <br> 24 hours | Number of <br> level scoops <br> per feed | Quantity of water per feed |  |
| :---: | :---: | :---: | :---: | :---: |
|  | less than $3 \cdot 5$ | 6 | 3 | 60 |
| $3 \cdot 5$ up to $4 \cdot 0$ | 6 | 4 | 90 | 2 |
| $4 \cdot 0$ up to $5 \cdot 0$ | 5 | 6 | 120 | 3 |
| $5 \cdot 0$ up to $6 \cdot 5$ | 5 | 7 | 150 | 4 |
| $6 \cdot 5$ up to $7 \cdot 5$ | 4 | 8 | 180 | 6 |
| $7 \cdot 5$ or more | 3 | 7 | 150 | 5 |

Each level scoop contains 4.5 g of milk powder.
Baby Andrew weighs $7 \cdot 1 \mathrm{~kg}$.
(d) Determine whether a 900 g pack of milk powder will last Andrew 1 week. Use your working to justify your answer.
8. A new road bridge has been built.

A worker paints 367 lines along the centre of the road.

- Each line is four metres long
- There is a gap of two metres between each line
- The first line starts at the beginning of the bridge
- The last line finishes at the end of the bridge
(a) Calculate the length of the bridge.

Two cables support a section of the bridge.
This section forms two right-angled triangles, as shown in the diagram.

(b) Calculate the total length of cable needed for this section of bridge. Do not use a scale drawing.
9. David is writing his new book.

He spends

- 210 hours on research
- 96 hours in meetings
- 234 hours writing the book.
(a) Construct a pie chart to illustrate this information.
(An additional diagram, if required, can be found on page 21.)
Time spent on each task


9. (continued)

The publishing company produced the following table to show all the tasks involved in publishing the book.

| Activity | Description | Preceding task |
| :---: | :---: | :---: |
| A | Illustrate cover | H |
| B | Write 1st draft | C |
| C | Research ideas | None |
| D | Edit book | B |
| E | Publish book | A,J,G |
| F | Re-work | D |
| G | Proof read | F |
| H | Choose title | B |
| I | Copyright | B |
| J | ISBN | I |

(b) Complete the diagram below to show the tasks.
(An additional diagram, if required, can be found on page 21.)

9. (continued)

The books are to be packed in boxes for transporting to the bookshops.
The dimensions of the book and the internal dimensions of the box are shown in the diagrams.


The books need to be laid with the front cover facing upwards in the boxes. They must all be aligned in the same direction.
(c) Calculate the maximum number of books that can be packed into each box.
9. (continued)

This is the fourth book that David has written in this series of books.
The cost of each book is shown in the table.

| Book | Cost | Year published |
| :---: | :---: | :---: |
| 1 | $£ 5 \cdot 50$ | 2013 |
| 2 | $£ 8 \cdot 50$ | 2015 |
| 3 | $£ 4 \cdot 00$ | 2016 |
| 4 | $£ 12 \cdot 00$ | 2019 |

The following special offers are available to buy all four books.

(d) Determine which shop offers the best deal for buying all four books. Use your working to justify your answer.
10. A sports ground is in the shape of a rectangle and two semi-circles as shown.


The running track is shaded in the diagram.
(a) Calculate the area of the running track.
10. (continued)

The running track is to be resurfaced.
A resurfacing company has a team of 5 workers who can resurface a track of this size in 42 hours.

The resurfacing company are now able to provide 2 more workers to resurface this track.

All the workers work at the same rate.
(b) Calculate the time it will now take to resurface the track.

## 10. (continued)

John works for the resurfacing company.
His annual salary is $£ 17108$.
National Insurance is calculated on a person's salary before deductions such as pension contributions.

| National Insurance rates |  |
| :--- | ---: |
| Up to $£ 8424$ | $0 \%$ |
| From $£ 8424$ to $£ 46384$ | $12 \%$ |
| Over $£ 46384$ | $2 \%$ |

(c) (i) Calculate John’s annual National Insurance payment.

John pays $7 \%$ of his annual salary into his pension. John's annual income tax is $£ 1051 \cdot 60$.
(ii) Calculate John's annual net pay.

Additional grid for use in question 7 (c) (i)

New-born babies: weight versus length


Additional diagram for use in question 9 (a)
Time spent on each task


Additional diagram for use in question 9 (b)



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